Slow-Neutron Capture: **Present Status and Outlook**

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Cornerstones of the *extreme* statistical model of γ decay

- Porter-Thomas distribution of partial radiation widths
- A notion of strength function (fragmentation of strength of simple nuclear states)
- The principle of the detailed balance
- Brink hypothesis
- ... and rather problematic absence of width correlation





Quantitatively: $k_{\gamma}^2 \sigma_{\gamma n} = k_n^2 \sigma_{n\gamma}$





Brink hypothesis

Photoexcitation pattern does not depend on initial excitation energy of a target nucleus



Brink hypothesis



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Photon strength functions: problems



Photon strength functions: problems



First hint for validity of Brink hypothesis



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First hint for validity of Brink hypothesis

L. M. Bollinger and G. E. Thomas, Phys. Rev. Lett. 18 (1967) 1143:

"There is no adequate, theoretically based explanation of the E_{γ}^{5} dependence of the experimental widths, although an idea introduced by Brink and developed by Axel may be relevant."

For Lorentzian E1 GDR

$$f^{(E1)}(E_{\gamma}) = \frac{1}{3 \ (\pi \hbar c)^2} \cdot \frac{\sigma_{\rm G} \, \Gamma_{\rm G}^2 \, E_{\gamma}}{(E_{\gamma}^2 - E_{\rm G}^2)^2 + E_{\gamma}^2 \, \Gamma_{\rm G}^2}$$

then for heavy nuclei

$$\frac{\mathrm{d}}{\mathrm{d}E\gamma} \ln f^{(E1)}(E_{\gamma}) \approx 2 \text{ at } E_{\gamma} \approx 7 \text{ MeV}$$

$$< I_{\lambda\gamma \mathrm{f}} >_{\lambda} \propto E_{\gamma}^{5}$$

... a statistical model for γ decay of neutron capturing states implications for *complete spectroscopy* of low-lying levels (ARC method)

Taken for granted for last 40 years

Widely accepted arguments in favor of Brink hypothesis

ARC data from ¹⁶⁷Er(n,γ)¹⁶⁸Er reaction: *detailed analysis*



W. F. Davidson et al., J. Phys. G 7 (1981) 455

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Reality

ARC data from 167 Er(n, γ) 168 Er reaction





Behavior of primary *M*1 transitions in ARC experiments

ARC data from 167 Er(n, γ) 168 Er reaction





*M*1 transitions below neutron threshold in another

experiment

(p,p') reactions at intermediate energies ($E_p \approx 200 \text{ MeV}$) at forward angles – provide information on *M*1 spin-flip transitions



- These transitions display marked resonant behavior
- Problems with determination of a full *M*1 strength
- So far, no serious comparison between (p,p') and (n, γ) data has been made

Models used for E1 PSF

1. Axel-Brink model:

$$f_{\rm AB}^{(E1)}(E_{\gamma}) = \frac{1}{3(\pi\hbar c)^2} \frac{\sigma_{\rm G} \ \Gamma_{\rm G}^2 \ E_{\gamma}}{(E_{\gamma}^2 + E_{\rm G}^2)^2 + E_{\gamma}^2 \ \Gamma_{\rm G}^2} \qquad \text{SLO model}$$



- Not justified for deformed nuclei
- At **7**>0 it gives a non-zero limit for $E_{\gamma} \rightarrow 0$
- Diverges for $E_{\gamma} \rightarrow E_{G}$

Models used for E1 PSF



4. Semi-empirical model EGLO:

$$f_{\rm EGLO}^{(E1)}(E_{\gamma}, T_f) = \frac{1}{3(\pi\hbar c)^2} \frac{\sigma_{\rm G} \ \tilde{\Gamma}_{\rm G}^2 \ E_{\gamma}}{(E_{\gamma}^2 + E_{\rm G}^2)^2 + E_{\gamma}^2 \ \tilde{\Gamma}_{\rm G}^2} + f_{\rm KMF}^{(E1)}(0, T_f)$$

$$\tilde{\tilde{\Gamma}}_{\mathbf{G}}(E_{\gamma}, T_f) = \left[k_0 + \frac{E_{\gamma} - E_{\gamma 0}}{E_{\mathbf{G}} - E_{\gamma 0}}(1 - k_0)\right] \frac{\Gamma_{\mathbf{G}}}{E_{\mathbf{G}}^2} \left(E_{\gamma}^2 + 4\pi^2 T_f^2\right)$$

 k_0 , $E_{\gamma 0}$ adjustable parameters

J. Kopecky, M. Uhl and R. E. Chrien, PRC 47 (1993) 312

A good description for spherical, transitional and deformed nuclei achieved at energies $E_{\gamma} > 6 \text{ MeV}$

Models for M1 PSF

1. The single-particle model A constant PSF

2. The spin-flip model

Analogous to AB model for E1 PSF Parameters deduced from the $(p,p'\gamma)$ data

3. The scissors-resonance temperature-independent model Photon strength assumed not to depend on nuclear temperature

$$f^{(M1,\text{SR})}(E_{\gamma}) = \frac{16\pi}{27(\hbar c)^3} \frac{E_0}{\arctan(2E_0/\Gamma_{\text{SR}})} \frac{\Gamma_{\text{SR}} E_{\gamma}}{(E_{\gamma}^2 + E_{\text{SR}}^2)^2 + E_{\gamma}^2 \Gamma_{\text{SR}}^2} \sum B(M1)^{\uparrow}$$

$$E_0 = \sqrt{E_{\rm SR}^2 - \Gamma_{\rm SR}^2/4}$$

F. Becvar et al., PRC52 (1995) 1278

Comparison between photonuclear and (n, γ) data

Lorentzian/Axel-Brink/GLO model





(n,γ) data: intensities of primary transitions from isolated neutron resonances

Comparison between photonuclear and (n,γ) data

Lorentzian/Axel-Brink/GLO model

Transitional or spherical nuclei: a not satisfactory agreement



(n,γ) data: intensities of primary transitions from isolated neutron resonances

Comparison between photonuclear, (n, γ) and $({}^{3}\text{He}, \alpha\gamma)$ data



¹¹⁷Sn: photonuclear reaction and ³He-induced emission

Agvaanluvsan *et al.* Phys. Rev. Lett. **102**, 162504 (2009)



Anomalous 7 MeV *M*1 resonance superimposed on GLO *E*1 GDR?

or

Suppression of the Lorentzian GDR?

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Conflict between the ³He-induced *γ***-emission and the KMF model**



Agvaanluvsan et al. Phys. Rev. Lett. 102, 162504 (2009)

Simulation of γ cascades by means of DICEBOX algorithm

Assumptions:

For nuclear levels below certain "critical energy" spin, parity and decay properties are known from experiments

Energies, spins and parities of the remaining levels are assumed to be a discretization of an *a priori* known level-density formula – a random discretization with the Wigner-type long-range level-spacing correlations

A partial radiation width $\Gamma_{i\gamma f}^{(XL)}$, characterizing a decay of a level *i* to a level *f*, is a random realization of a chi-square-distributed quantity the expectation value of which is equal to $f^{(XL)}(E_{\gamma}) E_{\gamma}^{2L+1}/\rho(E_i)$, where the PSFs $f^{(XL)}$ and the density ρ are also a priori known

Selection rules governing the γ decay are fully observed

Any pair of partial radiation widths $\Gamma_{i \not f}$ (XL) is statistically uncorrelated

Depopulating intensities are given by $I_{if} = \left[\sum_{XLf} \Gamma_{ivf}^{(XL)} \right] / \left[\sum_{X'Lf'} \Gamma_{ivf}^{(X'L')} \right]$

Siimulation of γ cascades by DICEBOX



Necessity to generate the rest part of the decay scheme

A straightforward approach to simulating γ cascades



Necessity to generate the rest part of the decay scheme

This problem is overcome by introduction of the so-called precursors

A notion of a nuclear realization

A set of realizations $\{I_{fi}\}$ for all possible *i*, *f* and a set of realizations $\{E_f, J_f, \pi_f\}$ for all levels *f*

A nuclear realization

- An infinite number of NRs exist for a given level-density ρ and a set of photon strength functions f^(XL)
- Of these NRs only one of characterizes the behavior of a given nucleus
- Simulations of γ cascades based on the use of various NRs lead to mutually different predictions of the cascade-related quantities
- Simulations of γ cascades based on the use of various NRs lead to different predictions of the cascade-related quantities
- To assess uncertainties of these predictions simulations of γ cascades are to performed for a large number of NRs

- The number of steps of a given cascade is known
 - So also the energies of the individual transitions and the intermediate levels involved
 - The procedure described is reiterated many times. Typically a set of 100 000 cascades are obtained for a given nuclear realization
 - -The whole this process in repeated for an enough large number of other nuclear realizations
 - Various *cascade-related quantities* can be deduced and their residual Porter-Thomas r.m.s. uncertainties estimated

Two-step γ -cascades following the thermal neutron capture



terminating at preselected final levels

Response function of the TSC HPGe spectrometer



GEANT3 simulation

- Virtually free of background
- γ-cross-talk negligible
- no need for deconvolution

Courtesy of Gencho Rusev

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An example of aTSC spectrum



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Specifity of TSCs terminating at 251 keV level

Role of scissors mode built on excited levels?

Allowed transitions E1 - E1 & M1 - M1favourable energy span $B_n - E_f \approx 2E_{SR}$

... effect of *co-operative* enhacement of primary and secondary transitions?

A unique possibility of a sensitive test for presence of SRs built on the levels in the quasicontinuum

Co-operative enhancement of primary and secondary transitions

Co-operativness -- what does it mean?





Co-operative enhancement of primary and secondary transitions

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TSCs in the ¹⁶²Dy(n, γ)¹⁶³Dy reaction



n-step cascades following the capture of keV neutrons in¹⁶²Dy

 $E_{\rm n}$ = 90-100 keV



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Comparison between the TSC and NRF data



Comparison between the TSC and NRF data II. NRF data for ¹⁶³Dy



Even if **all** ¹⁶³Dy transitions observed are *M*1 we get only $\Sigma B(M1)^{\uparrow} = 1.53 \mu_N^2$... while TSC ¹⁶³Dy data yield total $\Sigma B(M1)^{\uparrow} = 6.2 \mu_N^2$

A 3 MeV resonance seen from (${}^{3}\text{He},\alpha$) reactions in deformed nuclei



• A-dependence of SR energy differs differs from that observed from NRF data

- a "pygmy resonance" of an unknown multipolarity or the SR resonance?

- dependence of SR energy on energy of the level on which the SR resides?

Dependence of SR energy on energy of the level on which the SR resides?



It does not seem to be the case:

 the position of the 3 MeV peak is remarkably stable with changing the initial excitation

Data taken from A. Schiller et al., Physics of Atomic Nuclei 62 (2001) 1186

Populations of ¹⁰⁶Pd low-lying levels from thermal neutron capture in ¹⁰⁵Pd

Krtička et al., Phys. Rev. C 77, 054615 (2008) & D. De Frenne and E. Jacobs, Nucl. Data Sheets 72, 1 (1994)



Sensitivity of populations of low-lying levels to a spin makeup of the (thermal) neutron capturing state

¹⁰⁵Pd(n, γ)¹⁰⁶Pd reaction

Krtička et al., Phys. Rev. C 77, 054615 (2008) & D. De Frenne and E. Jacobs, Nucl. Data Sheets 72, 1 (1994)



Dynamic range: almost 3 orders !

Sensitivity of populations of low-lying levels to *E*1-to-*M*1 ratio of PSFs

¹⁰⁵Pd(n, γ)¹⁰⁶Pd reaction

Krtička et al., Phys. Rev. C 77, 054615 (2008) & D. De Frenne and E. Jacobs, Nucl. Data Sheets 72, 1 (1994)



A constant M1 PSF seems to be better ...

Populations of ⁹⁶Mo low-lying levels from thermal neutron capture in ⁹⁵Mo



Krtička et al., Phys. Rev. C 77, 054319 (2008) & Nuclear Data Sheets

- The spin makeup of neutron capturing state differs from that listed in BNL-325
- The agreement still far from being ideal misplaced levels?

Populations of ¹⁵⁰Sm low-lying levels from thermal neutron capture in ¹⁴⁷Sm

Shangwu Wang, et al., Nucl.Instr. Methods A 513, 585 (2003)



Problem of strong enhancement of strength of ⁹⁶Mo at low γ energies





Problem of strong enhancement of strength of ^{96}Mo at low γ .

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Problem of strong enhancement of strength of ⁹⁶Mo at low γ energies

Integrated TSC intensities

Simulations: Dipole PSF models with a full or restricted divergence at zero energies

Data: TSC experiment at Rez





Problem of strong enhancement of strength of ⁹⁶Mo at low γ

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Problem of strong enhancement of strength of ^{96}Mo at low γ



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TSC Final Level



Problem of strong enhancement of strength of ^{96}Mo at low γ

1. Rigorous analysis excludes the proposed Oslo PSFs at 99.8% confidence level.

Krticka *et al.*, Phys. Rev. C **77**, 054319 (2008)

- 2. The enhancement is very weak, if any.
- 3. Data from DANCE at isolated *s* and *p*-wave resonances confirm this conclusion

Essentials of γ **-calorimetric studies of** γ **cascades**



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Problem of strong enhancement of strength of ⁹⁶Mo at low γ energies

Data from the DANCE array v.s. simulations



Problem of strong enhancement of strength of ⁹⁶Mo at low γ energies

Data from the DANCE array v.s. simulations

Simulations:

the postulated PSFs used were identical to the "best PSFs" obtained by *trialand-error method* from analysis of Řež TSC data



SUMMARY

A deficit of photon strength in spherical and transitional nuclei at γ -ray energies of 6-8 MeV

Methods of TSCs and the *n*-step cascades (following the capture of keV neutrons or capture at isolated resonances) proved to be efficient tools for studying PSFs at intermediate γ -ray energies of 2 – 4 MeV

A strong evidence for scissors-like vibrations of *excited* deformed nuclei. The scissors M1 mode *per se* displays, indeed, resonance-like behavior

Very large values of the reduced $B(M1)\uparrow$ strength found; a deeper revision of the NRF data would be welcome

No meaningful enhancement of photon strength at low energies in ⁹⁶Mo has been found

With present knowledge of PSFs the populations of low-lying levels are predicted with success

Discrepancy between the data from the $^3\text{He-induced}\,\gamma$ emission and the KMF model

OUTLOOK

The role of nuclear temperature still not fully established. Measurements on a TSC setup with highly efficient multi-detector system installed on pure thermal neutron beam could shed more light on this key problem.

Future γ-calorimetric data from DANCE, n_TOF and J-Parc facilities may reveal possible presence of scissors mode in very heavy nuclei or even radioactive nucle

Co-operative efforts of NRF, (n,γ) and photonuclear communities may solve still open problems related to existence of pygmy resonances

Attention of theorists is needed for understanding the physics behind the suppression of the low-energy tail of the GDR

The very existence of the scissors resonances built on each excited level is a great challenge for microscopic nuclear theory. *The intuition of D. M. Brink is fascinating.* Finding the nature of this phenomenon may lead to prediction and discovery of new, so far, not known phenomena in behavior of medium-weight and heavy nuclei.

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TSCs in the 167 Er(n, γ) 168 Er reaction



TSCs in the 167 Er(n, γ) 168 Er reaction

